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Determination of porosity from shrinkage curves during sintering of granular materials

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ABSTRACT

This paper investigates the implementation of an analytical model to determine the porosity of a granular material during reactive and nonreactive sintering. A graphical interpretation of this model is proposed to calculate the porosity by comparing the experimental shrinkage curve with the ideal one. For the nonreactive sintering, some examples have been taken from the literature to illustrate the application of this method for two granular materials (alumina and zircon). In the case of reactive sintering, we have used our experiments to study the sintering behavior of magnesium hydroxide. The shrinkage curve was determined by dilatometer and the porosity was measured by helium pycnometer. The comparison revealed that the porosity calculated from the model is fully consistent with the porosity measurements in the both cases.

KEYWORDS

Graphical method; model; porosity; shrinkage; sintering

Introduction

Sintering can be described as the change of a powder compact in a coherent material under the action of heat. This industrial process is used in several areas such as biomedical material,^[1] fabrication of nuclear combustible,^[2] catalyst in sensors,^[3] etc.). It is considered as a very complex phenomenon because the fundamental mechanisms of sintering are still a matter of controversy.

The sintering process usually causes volume and surface change. In fact, atomic diffusion results in joining of the particles (formation of necks between grains,^[4] neck growth, rearrangement, grain growth with shrinkage, and deformation) and reduction of the porosity which is the main objective of sintering.

The control of these parameters (deformation, shrinkage, and porosity) is essential, to avoid post-treatment, to optimize, to better understand the sintering process, and therefore to improve the quality of the sintered components.

In many cases, there are chemical reactions of two or more components during sintering^[5–9]; in this case, the sintering allows the formation of a new chemical compound and its shrinkage.

For this, various techniques have emerged depending on the way of heating the powder. These techniques include natural sintering also called conventional

sintering (using an oven as a heating source)^[7,9,10] and nonconventional sintering such as microwave sintering (irradiation by a microwave field),^[9,11] sintering under load (compaction hot uniaxial or hot isostatic pressing),^[12,13] flash sintering also called SPS (applying a uniaxial pressure and an electric current),^[14–16] and laser sintering (scan a powder bed by a laser beam).^[17,18]

In the literature, many works have been presented to determine experimental parameters during sintering.^[19–21] Many products were studied like alumina,^[22,23] zircon,^[22] copper oxide,^[24,25] ceramics,^[19–21,26–28] titanium,^[29] and alloys.^[30] Parallely, numerous models have been developed taking into account the different mechanisms induced by sintering (particle size distribution effects, surface diffusion, particle coalescence, phase transformation, evaporation/condensation, etc.). These models are ranging from macroscopic (phenomenological) models to mesoscopic and microscopic (physical) ones. The microscopic model, also called two spheres model, is the first analysis of sintering and the simplest model.^[31–33] The micromechanical model can handle agglomeration, anisotropy, and particle grain size distribution, but it cannot directly model the effect of impurities and doping. Their influence on the microstructural evolution is reflected in the diffusion coefficient and interfacial energies.

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The mesoscopic models are based on simple geometries (like two or multisphere model). These models involve the mass transfer mechanisms during sintering and they are used to describe the evolution of microstructure during sintering,^[34] which determine the thermal, mechanical, and electrical properties at macroscopic scale.

The macroscopic models have been developed to simulate the shrinkage and the deformation during the sintering process. With these models, the temperature, mechanical, and densification properties of the sintered compacts can be described by developing a constitutive law based on the continuum mechanics of porous media.^[35–37]

In the literature, some numerical models^[8,38–43] describing the shrinkage and the porosity change during sintering have been validated by experiments. Ou et al.^[38] studied the sintering behavior of microbimaterial components during a powder injection molding with dilatometry experiments and gravitational beam bending. As a complement to their experimental study, a thermoelastoviscoplastic model was developed and simulated by finite element method. The simulations were based on constitutive equations identified from specific experiments performed for each blend at different sintering heating rates and loadings. Maca et al.^[39] developed a new automatic procedure to recalculate dilatometric shrinkage data to plot density as a function of time and temperature. Maizza et al.^[40,41] have proposed a numerical/experimental methodology. Their experimental part is based on experiments of SPS sintering on pure and ultrafine tungsten carbide powder. The developed model is a thermoelectric model taking into account the shrinkage phenomenon. A comparison between shrinkage curves and the numerical and experimental temperatures was used to test the model developed and to estimate all the unknown variables (density, heat capacity, thermal diffusivity). Li et al.^[42] have determined experimentally the sintering behavior of TiO_2 monomodal porous compacts containing intergranular pores and bimodal porous scaffolds prepared by freeze casting, containing small intergranular pores and large interlamellar pores, then they compared the obtained results with those examined by finite element analysis. Wei et al.^[43] have used a model known as power-law creep of powder to describe the densification mechanism of zirconium carbide (ZrC) powder under SPS. The numerical solution of this model is compared to the obtained experimental data in the inverse regression process to evaluate the power-law creep coefficients of the ZrC powder.

Modeling can help estimate and better optimize the process parameters. In this context, the aim of the

present work is to develop a general model based on a graphical interpretation to determine the porosity from the experimental and ideal shrinkage curves during sintering. The graphical interpretation was used in our previous work^[44] to determine porosity during drying. In the literature, several works, allowing to calculate the porosity from the shrinkage during drying,^[45–49] have been presented.

During sintering, the proposed analytical models in the literature^[32,33] can only treat complex diffusion and transport mechanisms. The prediction of the porosity from shrinkage has been processed numerically.^[38,43]

Model formulation

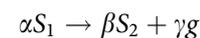
A granular material, composed of solid matrix and air, with an initial volume V_0 , initial mass m_0 , initial bulk density ρ_0 , and initial porosity ε_0 , is sintered under controlled conditions.

At time instant t , the volume is V , the density is ρ , the mass is m , and the porosity is ε . We suppose that volumes of solid and air phases are additive and the mass of air phase is negligible with respect to the mass of solid.

We will treat two cases of sintering: the reactive and the nonreactive sintering.

Reactive sintering

We consider that a solid S_1 , undergoing a thermal process, is reacted to give a solid S_2 and gas according to the following chemical reaction:



where α , β , and γ are the stoichiometric coefficients.

Initially (at $t = 0$), the number of moles of the solid S_1 is n_0 and the mass of the solid m_0 is given by the following expression:

$$m_0 = n_0 M_0 \quad (1)$$

where M_0 is the initial molar mass.

During the thermal process, the chemical reaction occurs, the number of moles of the reactant S_1 decreases to $n_0 - n$. Considering the material balance of the system, the number of moles of S_1 is transformed into several moles $\frac{\beta}{\alpha} n$ of the solid S_2 and $\frac{\gamma}{\alpha} n$ of gas.

where n is the number of moles decreasing from the solid S_1 at time instant t .

The masses m_{s1} and m_{s2} of the solids S_1 and S_2 are, respectively, given by the following equations:

$$m_{s1} = (n_0 - n) M_{s1} \quad (2)$$

$$m_{s2} = \frac{\beta}{\alpha} n M_{s2} \quad (3)$$

where M_{s1} and M_{s2} are, respectively, the molar mass of the solid S_1 and S_2 .

The bulk density at the beginning of the chemical reaction is expressed as:

$$\rho_0 = \frac{m_0}{V_0} = \frac{m_{s1}}{V_0} = \frac{m_{s1}}{V_{s1}} \cdot \frac{V_{s1}}{V_0} \quad (4)$$

$$\rho_0 = \frac{m_{s1}}{V_{s1}} \cdot \frac{(V_0 - V_a)}{V_0} \quad (5)$$

Thus:

$$\rho_0 = (1 - \varepsilon_0) \rho_{s1} \quad (6)$$

where ρ_{s1} is the solid density of the solid S_1 and ε_0 is the initial bulk porosity.

During the heating cycle, the bulk density is given by:

$$\rho = \frac{m}{V} = \frac{m_{s1} + m_{s2}}{V_{s1} + V_{s2}} \cdot \frac{V_{s1} + V_{s2}}{V} \quad (7)$$

$$\rho = \frac{(m_{s1} + m_{s2}) \cdot \rho_{s2}}{m_{s1} \rho_{s2} + m_{s2} \rho_{s1}} (1 - \varepsilon) \rho_{s1} \quad (8)$$

After development, we obtain the following expression:

$$\rho \left(1 - \frac{m_{s2}}{m} \left(\frac{\rho_{s2} - \rho_{s1}}{\rho_{s2}} \right) \right) = (1 - \varepsilon) \rho_{s1} \quad (9)$$

where ρ_{s2} is the solid density of the solid S_2 and ε is the bulk porosity.

Knowing that:

$$\frac{\rho}{\rho_0} = \frac{m}{m_0} \frac{V_0}{V} \quad (10)$$

And introducing the parameter Δ defined as $\delta = \frac{\rho_{s2} - \rho_{s1}}{\rho_{s2}}$, Eqs. (6), (9) and (10) can be combined to yield:

$$\frac{(1 - \varepsilon)}{(1 - \varepsilon_0)} \frac{V}{V_0} = -K + (1 + K) \frac{m}{m_0} \quad (11)$$

With

$$K = \frac{\beta M_2 \delta}{\beta M_2 - \alpha M_1} \quad (12)$$

where M_{s1} and M_{s2} are, respectively, the molar mass of the solids S_1 and S_2 .

The parameters governing the shrinkage are the solid density, molar mass of the two solids (reactant and product), and the stoichiometric coefficients of the chemical reaction.

From Eq. (11), we deduce that the shrinkage $\frac{(1-\varepsilon)}{(1-\varepsilon_0)} \frac{V}{V_0}$ varies linearly with the reduced mass loss $\frac{m}{m_0}$.

Two basic cases can be examined:

Case (a): Ideal shrinkage with initial porosity; $\varepsilon = 0$, $\varepsilon_0 \neq 0$

In this case, the ideal shrinkage curve y can be written from the Eq. (11) in the form:

$$y = \frac{V}{V_0} = (1 - \varepsilon_0) \left(-K + (1 + K) \frac{m}{m_0} \right) \quad (13)$$

Case (b): The general case: Nonideal shrinkage with initial porosity; $\varepsilon \neq 0$, $\varepsilon_0 \neq 0$

In general case, Eq. (11) is reduced to:

$$(1 - \varepsilon)z = (1 - \varepsilon_0) \left(-K + (1 + K) \frac{m}{m_0} \right) \quad (14)$$

where z is a dimensionless parameter representing the experimental shrinkage curve for a product.

The porosity can be easily deduced from Eqs. (13) and (14) and given by:

$$\varepsilon = \frac{z - y}{z} \quad (15)$$

A graphical interpretation of Eq. (15) is shown in Fig. 1a where the porosity is equal to the ratio of the

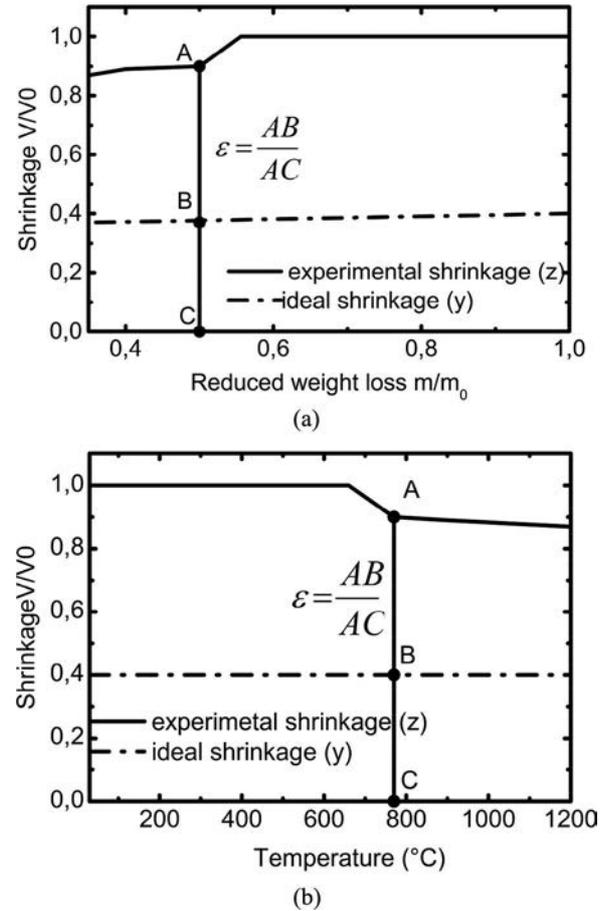


Figure 1. Determination of porosity using visual interpretation of the shrinkage curves for: (a) nonreactive sintering and (b) reactive sintering.

segment AB to segment AC .

$$\varepsilon = \frac{AB}{AC} \quad (16)$$

Nonreactive sintering

In the case where sintering is not preceded by a chemical reaction, the shrinkage will be deduced from Eq. (11) with $m = m_0$ and $K = 0$, thus leading to the following equation:

$$\frac{1 - \varepsilon}{1 - \varepsilon_0} = \frac{V_0}{V} \quad (17)$$

From Eq. (13), the ideal shrinkage coefficient becomes a constant:

$$y = 1 - \varepsilon_0 \quad (18)$$

Two properties measured at the beginning and at the end of the experiment (initial porosity ε_0 and initial volume V_0) are necessary for the full description of the model.

The porosity change can easily be deduced from Eq. (15).

As the reactive case, the graphical interpretation can be used to determine the porosity (Fig. 1b).

The porosity thus depends on the experimental values of the shrinkage and on set of properties (initial bulk density and solid density).

Materials and methods

High-purity magnesium hydroxide powder (Sigma-Aldrich, 95%) with an average granule size of $2.86 \mu\text{m}$ (the particle size dimension of the powder was measured by Microtrac S3500) was used in all experiments.

The powder was uniaxially pressed at 10^{-1} Mpa, for 240 s, into 6 mm diameter cylindrical porous compacts and various thickness. The porosity in the green state (initial porosity), $\varepsilon_0 \approx 71\%$, was calculated from the geometric volume and the true volume, considering the true density measured by the helium pycnometer for $\text{Mg}(\text{OH})_2$.

The green compact was sintered at various temperatures (from 400 to $1,350^\circ\text{C}$) using a Nabertherm furnace. The heating and cooling rates were, respectively, 10 and $30^\circ\text{C min}^{-1}$ with a holding time of 60 min at 400°C .

At 400°C (the decomposition temperature), the samples before and after sintering were weighted and examined by structural analysis with X-ray diffraction (XRD) in a X'PERT Pro MPD PANALYTICAL

diffractometer, using a $\text{CuK}\alpha$ radiation ($\lambda = 1.540060 \text{ \AA}$). The crystallite size was determined by XRD through the full width at half-maximum (FWHM) of the (2θ) Bragg peak using the formula:

$$\tau = d\lambda / (G \cos \theta) \quad (19)$$

where τ is the FWHM, λ is the X-ray wavelength, G is the crystallite size, θ is the diffraction angle, and d is the Scherrer constant to account for the particle shape (close to unity, normally 0.9).

The crystalline phases were identified by reference to the International Center for Diffraction Data.

Differential thermal analysis and thermogravimetry were performed using 28.7 mg of powder with a DTA-TG SETARAM SETSYS Evolution-1750. Linear shrinkage was determined by dilatometry (SETARAM SETSYS Evolution-1750) using the same thermal cycle as for DTA.

Apparent and true densities were measured using helium pycnometer (Accu Pyc II 1340, Micromeritics), and the bulk material density of the body was calculated from the weight and geometrical dimensions.

In this study, open, closed, and total porosities are calculated according to the following formulas:

$$\varepsilon_{\text{closed}} = 1 - \frac{\rho_{\text{app}}}{\rho_{\text{true}}} \quad (20)$$

$$\varepsilon = 1 - \frac{\rho_{\text{bulk}}}{\rho_{\text{true}}} \quad (21)$$

$$\varepsilon_{\text{open}} = \varepsilon - \varepsilon_{\text{closed}} \quad (22)$$

To track the porosity change, the microstructures of the sintered specimens were observed by scanning electron microscopy (SEM) (JEOL JSM-5400). The pre-sintered and sintered samples were fractured and gold sputtered before examination.

Results and discussion

To calculate porosity, we applied the shrinkage model for two nonreactive materials (alumina and zircon) sintered under free sintering. The data were collected from Falamaki et al.^[22] (Table 1). For these materials, two properties were listed: the bulk initial density and the solid density (Table 2).

The experimental works of Falamaki et al.^[22] were used for the application of the model for alumina and zircon to calculate porosity changes during sintering.

Fig. 2 shows the experimental data from Falamaki et al.^[22] with the experimental values of solid density and initial bulk density; an initial porosity ε_0 was calculated (Table 2) allowing the calculation of the ideal shrinkage.

Table 1. Sintering conditions and material properties from the reference used in the application of present porosity estimation model (Eq. (17)).

Product	Techniques and conditions of sintering		Measured properties	Measured apparatus	Reference
	Techniques	Conditions (heating program)			
Alumina	- Uniaxial pressing (forming pressure 31.2 MPa) - No binder addition	- Heating up to 1,000°C with a heating rate of 20°C min ⁻¹	- Porosity	- ASTM C 373-88	Falamaki et al. ^[22]
Zircon	- Uniaxial pressing (forming pressure 31.2 MPa) - Addition of 4 wt% PVA - Firing in air atmosphere	- Heating up to the sintering temperature with a heating rate of 5°C min ⁻¹ - 1 h soaking time	- Shrinkage	- Dilatometer Setaram 16/18	

Table 2. Properties of the studied granular materials used in the application of present model.

Product	Initial bulk density (kg m ⁻³)	Solid density (kg m ⁻³)	Initial calculated porosity (%)
Alumina	2,300	4,000	0.425
Zircon	2,400	4,800	0.5
Magnesium hydroxide	795.403	2,360	0.662
Magnesium oxide	-	3,580	-

Equation (15) allows determining porosity during the whole sintering process.

The calculated porosity curve (Figs. 3 and 4) shows the same form as experimental porosity of Falamaki et al.^[22] for both cases (alumina and zircon products). We observe that at the initial stage of sintering (for small values of the temperature $T < 1,300^\circ\text{C}$), the calculated porosity obtained from the proposed model is quite different compared to the measured porosity. The difference may be due to the microstructure of the sample and measurement errors. In fact, in general, in the initial stages of sintering, pore growth may occur by different mechanisms such as particle coalescence, particle size distribution effects, surface diffusion. The result is some kind of particle rearrangement in the initial step of sintering. Some groups of relatively small

highly compact aggregates shrink on themselves by particle rearrangement with neck growth, resulting in the growth of irregular voids caused by the separation between the shrinking groups.

During this first stage, shrinkage is minimal and porosity decreases only slightly.

A transition zone (at higher sintering temperatures beginning from $T = 1,350^\circ\text{C}$) may be observed in the porosity and in the experimental shrinkage versus temperature curves for alumina and zircon as well.

Within this transition zone, the densification process undergoes acceleration and shrinkage and porosity becomes significant.

The model was tested for a reactive product (the magnesium hydroxide). The XRD patterns of the initial and free sintered powder are given in Fig. 5. The XRD diffraction pattern of the initial powder reveals only peaks of $\text{Mg}(\text{OH})_2$ called brucite. At 400°C , the $\text{Mg}(\text{OH})_2$ was decomposed; the phase composition of the sample sintered at 400°C consists of magnesium oxide (called periclase): the following thermal reaction which takes place is:

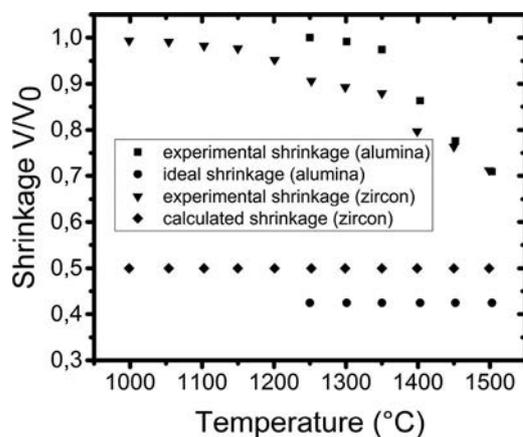
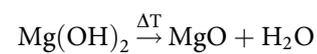


Figure 2. Free nonreactive sintering of alumina and zircon: ideal shrinkage (calculated using Eq. (18)) and experimental shrinkage curves (Falamaki et al.^[22]).

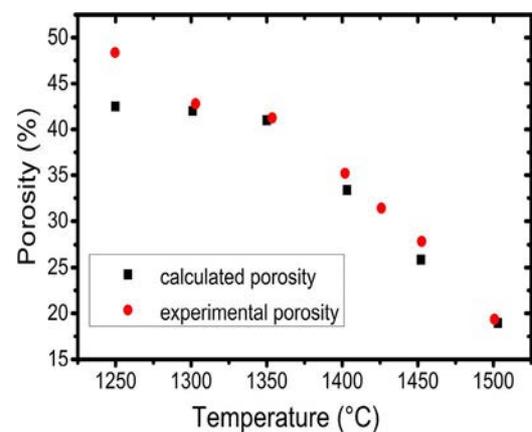


Figure 3. Free nonreactive sintering: comparison of calculated porosity (■) from Eq. (15) by referring to Table 2 and experimental porosity of alumina (●: Falamaki et al.^[22]).

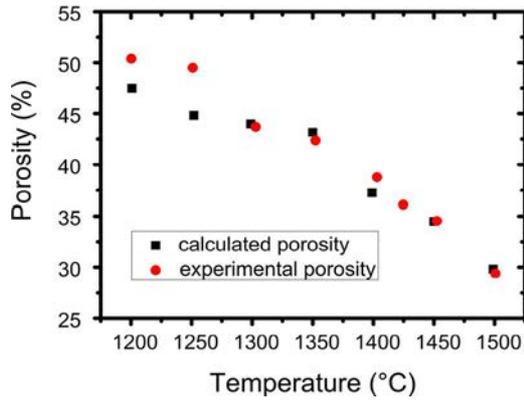


Figure 4. Free nonreactive sintering: comparison of calculated porosity (■) from Eq. (15) by referring to Table 2 and experimental porosity of zircon (●: Falamaki et al.^[22]).

The study of thermal behavior of the initial and sintered powder has proved to be a powerful way for understanding physical phenomena during sintering. Dilatometric analysis, differential and gravimetric analysis were used.

A feature that is interpreted from Fig. 6 is the bulk shrinkage coefficient of compacts. The bulk shrinkage coefficient is related to the linear shrinkage $\left(\frac{L-L_0}{L_0}\right)$ measured by the dilatometer by the relation:

$$\frac{V}{V_0} = \left(1 + \frac{L - L_0}{L_0}\right)^3 \quad (23)$$

Dilatometric analysis was performed at 1,400°C. If shrinkage behavior is evaluated considering microstructural evaluation, three main stages are observed in the system.

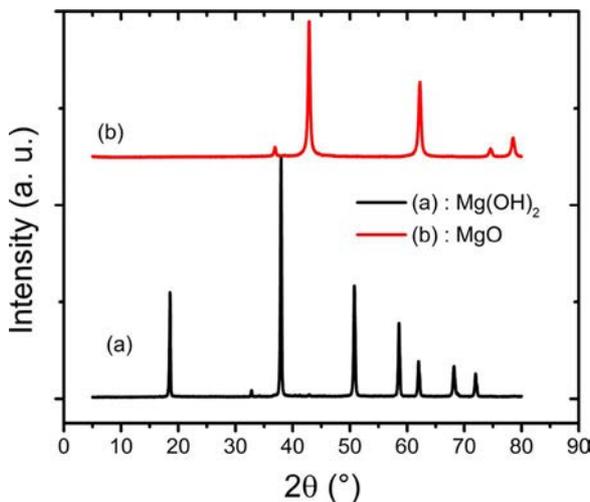


Figure 5. XRD spectrums of $Mg(OH)_2$ sintered at various temperatures: (a) 30 and (b) 400°C. Note: XRD, X-ray diffraction.

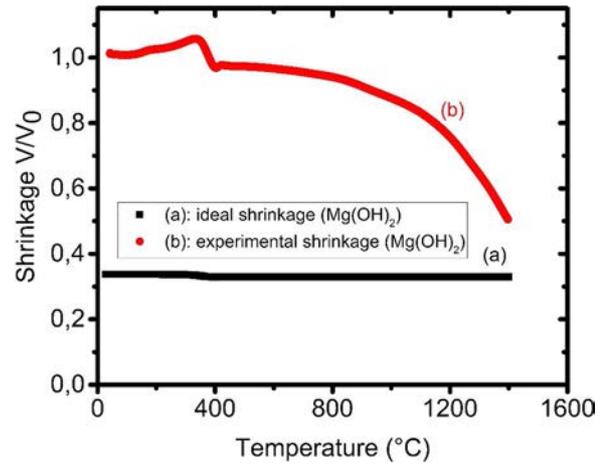


Figure 6. Experimental (b) and ideal shrinkage (a) calculated using Eq. (13) as a function of temperature for free reactive sintering ($Mg(OH)_2$).

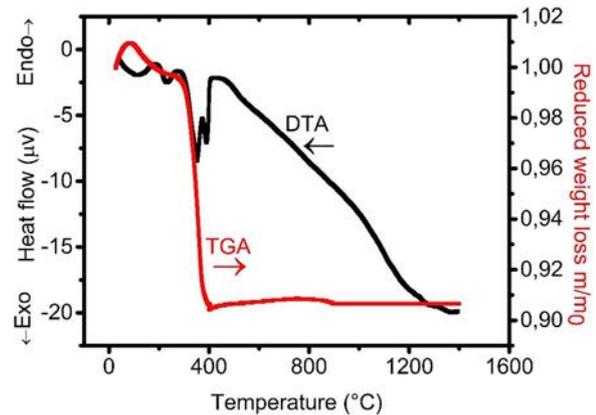


Figure 7. DTA and TGA thermograms of $Mg(OH)_2$.

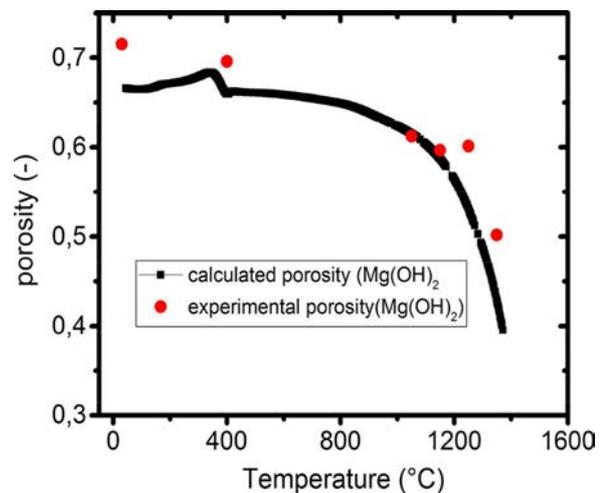


Figure 8. Free reactive sintering: comparison of calculated porosity (■) using Eq. (15) and referring to Table 2 and experimental porosity (●) of magnesium hydroxide.

In the first stage, volumetric expansion is dominant and the grains grow larger (exaggerated grain growth). In the second stage, the microstructural evaluation is more complicated as sintering shrinkage is more effective because thermal activation is enough to join particles together and develop the neck formation between them. When the transformation is completed (third stage), shrinkage is dominant because sintering takes place for densification.

The decomposition path of $\text{Mg}(\text{OH})_2$ was studied by DTA/TGA analysis (Fig. 7). Two endothermic peaks were observed. The small endothermic peak below 250°C with a weight loss of 1.4% is related to the dehydration process. The second peak (at 400°C) which

corresponds to the decomposition reaction was very strong with a weight loss of 10.71%.

The data in Fig. 8 show that the measured porosity is in concordance with that obtained by the proposed method which confirms the validity of the model in case of reactive sintering.

The SEM images of $\text{Mg}(\text{OH})_2$ sintered at various temperatures (30, 400, 1,050, 1,150, 1,250, $1,350^\circ\text{C}$) are reported in Fig. 9. The surface fractures reveal an apparent change in the sample microstructure. At 30°C , the sample presents an important intergranular porosity which disappears partially when the temperature increases (Fig. 9). We can also notice the absence of intragranular porosity from the beginning, so it can

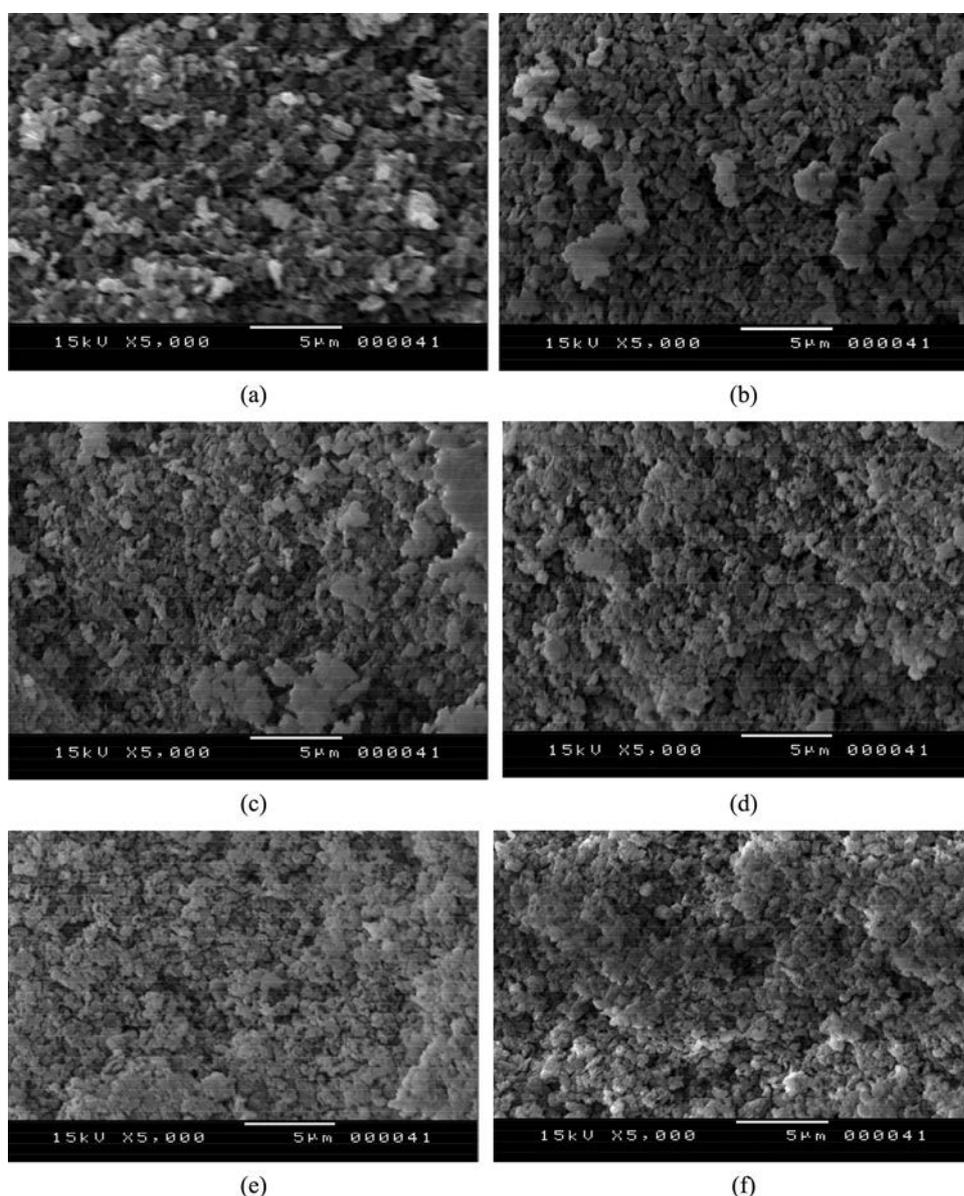


Figure 9. SEM micrographs of magnesium hydroxide samples sintered at different temperatures: (a) 30, (b) 400, (c) 1,050, (d) 1,150, (e) 1,250, and (f) $1,350^\circ\text{C}$. Note: SEM, scanning electron microscopy.

Table 3. Total and closed porosities of Mg(OH)₂ measured by pycnometry, balance and calipers, and open porosity calculated using Eq. (22) at different temperatures.

Temperature (°C)	Total porosity	Closed porosity	Open porosity
30	0.71341	0.00209	0.71132
400	0.695537	0.003455	0.692082
1,050	0.612205	0.0627	0.549505
1,150	0.596698	0.07165	0.525048
1,250	0.601181	0.062901	0.53828
1,350	0.502	0.062901	0.439099

be assumed that powder porosity is opened which was confirmed by the values of porosity measured by pycnometry (Table 3).

Microstructure of the Mg(OH)₂ sintered at 400°C (decomposition reaction) was characterized by the formation of clusters of particles; this agglomeration becomes more important at 1,350°C and, at this temperature, the density increases.

Thus, the results due to the microphotography are consistent with the values of intragranular, intergranular, and total porosities obtained by the model and by the experimental measurements.

Conclusion

In the frame of this study, an analytical model for determining the porosity during reactive and nonreactive sintering using a limited number of parameters identified with specific experiments (shrinkage, initial porosity, and weight loss) was proposed. This model, based on a graphical interpretation of the shrinkage curves to determine the variation of porosity, was applied to experimental data from the literature for the nonreactive sintering and ad hoc experiments for the reactive sintering.

For the case of nonreactive sintering, a transition zone is observed at the initial stage of sintering. Afterward, the densification process dominates and at 1,500°C, a quite dense product is obtained. A difference was observed between the calculated and experimental porosities. This difference is due to the microstructure sample and the error measurements.

For the reactive sintering, a microstructural analysis was performed to evaluate the microstructure of the magnesium hydroxide. The observations of microphotographs are consistent with the porosities obtained from the model and the experimental measurements. A slight difference between experimental and calculated porosities was observed. This difference can be attributed to the experimental device or measurement errors.

It can be concluded that the graphical interpretation which is a continuous and nondestructive method can be an efficient way to compute porosity from mass balances without using porosity measurement.

Nomenclature

m	mass (kg)
n	number of moles (mol)
M	molar mass (kg mol ⁻¹)
V	volume (m ³)
L	length (m)
T	temperature (°C)
γ	ideal shrinkage coefficient (-)
z	experimental shrinkage coefficient (-)
G	crystallite size (μm)
g	gas
d	the Scherrer constant (-)

Greek letters

ε	bulk porosity (-)
ρ	bulk density (kg m ⁻³)
τ	Full width at half maximum (-)
λ	wavelength (Å)
θ	diffraction angle (°)
α	stoichiometric coefficient
β	stoichiometric coefficient
γ	stoichiometric coefficient

Subscripts

0	initial
s	solid
a	air
App	apparent

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